

South Gosforth First School


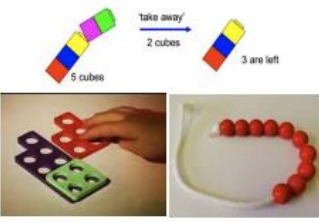
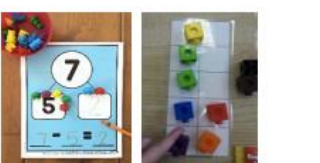
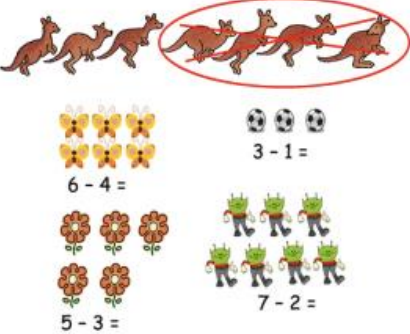
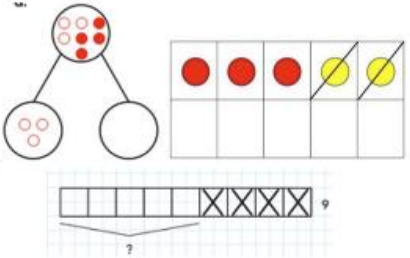

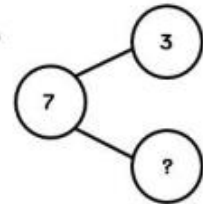
'Roots to grow and wings to fly'





Calculation Progression


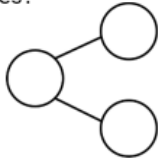

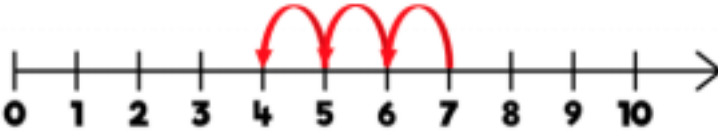




Subtraction

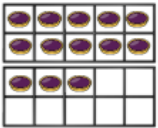
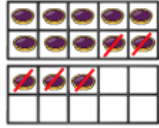
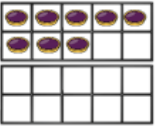
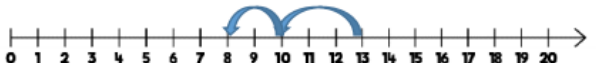
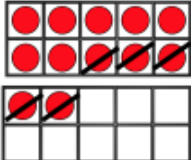
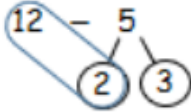
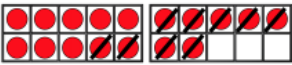
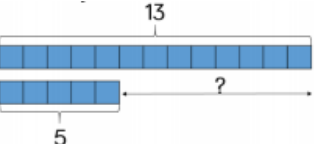
EYFS

Early Learning Goals	Models and Representations - CPA				
<p>Number ELG</p> <ul style="list-style-type: none"> - Have a deep understanding of number to 10, including the composition of each number - Subitise (recognise without counting) up to 5 - Automatically recall number bonds up to 5 (including subtraction facts) and some bonds to 10, including double facts. 	<div data-bbox="813 467 1198 691">  <p>Use toys and general classroom resources for children to physically manipulate, group/regroup.</p> </div> <div data-bbox="835 707 1153 930">  <p>Use specific maths resources such as snap cubes, Numicon, bead strings etc.</p> </div> <div data-bbox="857 994 1176 1249">  <p>Use visual supports such as ten frames, part part whole and subtraction mats, with the physical objects and resources that can be manipulated.</p> </div> <div data-bbox="1216 467 1624 802">  <p>A group of pictures for children to cross out or cover quantities to support subtraction.</p> </div> <div data-bbox="1216 898 1624 1157">  <p>Use visual supports such as ten frames, part part whole and bar model with pictures/icons.</p> </div> <div data-bbox="1624 499 2049 1233"> <p>A focus on symbols and numbers to form a calculation.</p>  <div data-bbox="1758 790 2049 885"> $10 - 6 = 4$ </div> <table border="1" data-bbox="1624 901 1915 1013"> <tr> <td>3</td> <td>?</td> </tr> <tr> <td colspan="2">7</td> </tr> </table> <p>$7 - 3 = ?$</p>  </div>	3	?	7	
3	?				
7					










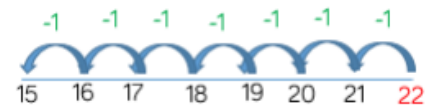
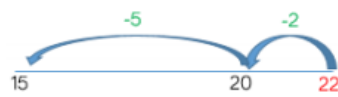
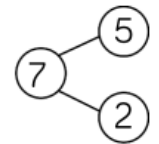
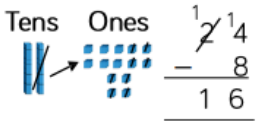
Year 1

Objective and Strategy	Models and Representations - CPA
<p>Subtraction within 10</p> <p>Taking away, how many left?</p> <p>Children are first introduced to the language of subtraction, rather than the subtraction symbol straight away. Taking away is used in a range of real life contexts such as flying away and eating.</p> <p>The use of zero is important so that children know when nothing is taken away the whole remains the same.</p>	<p>Complete the sentences to create a story and draw a part-whole model.</p> <div data-bbox="936 491 1220 619"> </div> <p>At first there were ___ apples. Then ___ were eaten. Now there are ___ apples.</p> <p>Write a story to go with the pictures and draw a part-whole model.</p> <div data-bbox="824 751 1227 858"> <p>First:  Now: </p> </div>
<p>Subtraction within 10</p> <p>Taking away, how many left? Introducing the subtraction symbol</p> <p>Children continue to use concrete and pictorial representations, alongside the use of the subtraction symbol, to deepen their understanding.</p>	<div data-bbox="1048 970 1512 1029"> </div> <p>$7 - 2 = \underline{\quad}$</p> <p>At first there were 10 bananas. 7 of them were eaten. How many bananas are left?</p> <p>Use counters/cubes to help you solve and complete:</p> <div data-bbox="824 1182 1025 1236"> $\square - \square = \square$ </div> <div data-bbox="1120 1145 1249 1278"> </div>

<p>Subtraction within 10</p> <p>Finding a part</p> <p>Children continue to use the subtraction symbol. Building on their understanding of finding a part, they are introduced to subtraction by partitioning.</p>	<p>How many ice creams do not have flakes?</p>  $6 - 2 = \underline{\quad}$  <p>There are $\underline{\quad}$ ice creams that do not have flakes.</p> <p>In total there are 8 counters. How many counters are there in the bag? Show this in a part-whole model and as a calculation.</p> 
<p>Subtraction within 10</p> <p>Counting back</p> <p>Children count backwards to subtract, which is an important step to help children work in the abstract.</p>	 $7 - 3 = \underline{\quad}$ $7 - 3 = \underline{\quad}$ $5 - 0 = \underline{\quad}$
<p>Subtraction within 10</p> <p>Finding the difference</p> <p>Children explore finding the difference as a form of subtraction. They could use their skills of counting back and counting on to help them to find the difference. Alternatively, they can make both amounts and visually see how many more/less a number is.</p>	<p>Whitney </p> <p>Teddy </p> <p>Whitney has $\underline{\quad}$ more cakes than Teddy.</p> $7 - 3 = \underline{\quad}$ <p>What's the difference between 10 and 6? </p> <p>The difference between 10 and 6 is $\underline{\quad}$ </p> $10 - 6 = \underline{\quad}$

<p>Subtracting – Crossing 10 (1)</p> <p>Children will be introduced to subtraction where they have to cross ten. This strategy focuses on partitioning to make ten.</p> <p>Children represent this using concrete manipulatives or pictorially with ten frames and number lines and will move towards using this as a mental strategy.</p>	<p>First there were 13 jam tarts</p>  <p>Then 5 were eaten</p>  <p>Now there are 8 jam tarts.</p>   <p>Rosie has used the ten frames to calculate $12 - 5$</p>   <p>$10 - 3 = 7$</p>
<p>Subtraction – Crossing 10 (2)</p> <p>Children subtract numbers, within 20, crossing 10 using the different structures of subtracting (taking away, partitioning, difference).</p> <p>They continue to use concrete manipulatives and pictorial methods to support their understanding.</p>	<p>Complete the number sentences to describe what happens to the sweets.</p>  <p>First there were ___ sweets. Then ___ sweets were eaten. Now there are ___ sweets.</p> <p>$\square - \square = \square$</p>  <p>$\square - \square = \square$</p>
<p>Further Notes</p>	<ul style="list-style-type: none"> Children will continue to count regularly on and back from different numbers in 1s and in multiles of 2, 5 and 10. Children will be encouraged to learn number bonds to 20 and experience the = sign in different positions. Children should see addition and subtraction as related operations eg $6 + 4 = 10$ which is related to $10 - 4 = 6$. Children will continue to practise fluency in subtraction facts within 10 which will support subtraction with 2-digit numbers in Year 2.

Year 2

Objective and Strategy	Models and Representations - CPA								
<p>Subtract 10s</p> <p>Children make use of place value to add and subtract 10s from a given number within 100. The focus is the importance of the tens digit within the given number and children should be encouraged to see the relationship.</p> <p>Children may also make connections between one-digit facts and 2-digit calculations.</p>	<table border="1"> <thead> <tr> <th>Tens</th><th>Ones</th></tr> </thead> <tbody> <tr> <td></td><td></td></tr> <tr> <td></td><td></td></tr> <tr> <td></td><td></td></tr> </tbody> </table> $\begin{array}{r} 56 \\ - 30 \\ \hline \end{array}$	Tens	Ones						
Tens	Ones								
									
									
<p>Subtract 1-digit from 2-digits- crossing ten</p> <p>Children need to be able to count to 20 and need to be able to partition two-digit numbers in order to subtract from them. They need to understand the difference between one-digit and two-digit numbers and line them up in columns.</p> <p>In order to progress to using the number line more efficiently, children need to be secure in their number bonds.</p>	<p>$22 - 7 =$</p>  <p>Can you put the larger number in your head and count back the smaller number? Start at 22 and count back 7</p> <p>Can we use number bonds to subtract more efficiently?</p>  <p>We can partition 7 into 5 and 2 and use this to bridge the 10</p> <p>Subtract 8 from 24</p>   $\begin{array}{r} 24 \\ - 8 \\ \hline 16 \end{array}$								

Subtract a 2-digit number from a 2-digit number not crossing ten

This is an important step before children start to look at subtraction where they cross a tens boundary. Children can first learn to subtract multiples of ten and then ones from a two-digit number, using a partitioning method.

They may then move on to a formal written method, using Base 10 equipment to support the calculation.

$$78 \text{ minus } 34 = \underline{\quad}$$

$$8 \text{ ones} - 4 \text{ ones} = \underline{\quad}$$

$$7 \text{ tens} - 3 \text{ tens} = \underline{\quad}$$

We have tens and ones.

Tens	Ones

$$34 - 13 = \underline{\quad}$$

$$\begin{array}{r} 34 \\ -13 \\ \hline 20 \end{array}$$

Subtract 13 from 28



$$\begin{array}{r} 28 \\ -13 \\ \hline 15 \end{array}$$

Subtract a 2-digit number from a 2-digit number – crossing ten – subtract ones and tens

Children use their knowledge that one ten is the same as ten ones to exchange when crossing a ten in subtraction. As with the previous step flexible partitioning is used as a method when the children are calculating with exchanges.

Children use concrete manipulatives (such as Base 10) and pictorial representations (such as number lines and part whole models) to develop their understanding and may move to recording this using the written columnar method.

Tens	Ones

$$\begin{array}{r} 5 \quad 1 \\ 65 \\ -28 \\ \hline 37 \end{array}$$

Tens	Ones

$$63 - 17 = 46$$

$$\begin{array}{r} 63 \\ -17 \\ \hline 46 \end{array}$$

$$63 - 10 = 53$$

$$53 - 7 = 46$$

$$63 - 17 = 46$$

$$\begin{array}{r} 63 \\ -17 \\ \hline 46 \end{array}$$

$$63 - 7 = 56$$

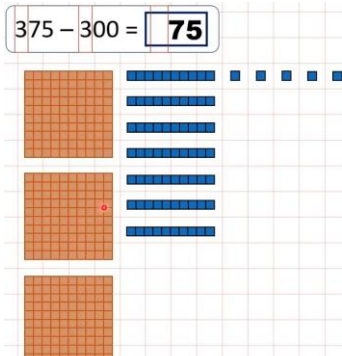
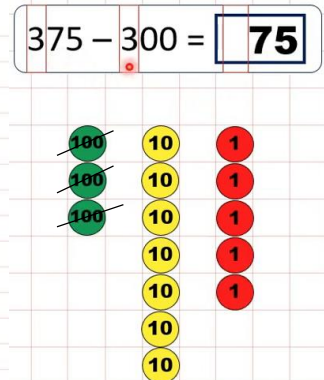
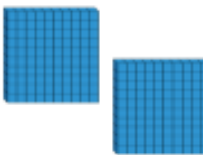


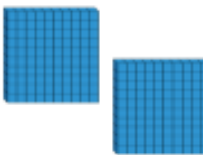


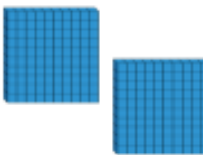


$$56 - 10 = 46$$

Further Notes

- Children will be counting regularly, on and back, in steps of 2, 3, 5 and 10. Counting back in tens from any number will link with subtracting multiples of 10.
- Children will practise subtraction to 20 to develop fluency and will be encouraged to use the facts they know to derive others eg using $10 - 8 = 2$ and $8 = 10 - 2$ to calculate $100 - 80 = 20$ and $80 = 100 - 20$.
- Children will learn to check their calculations using a range of strategies, including by using the inverse method of addition to check a subtraction.

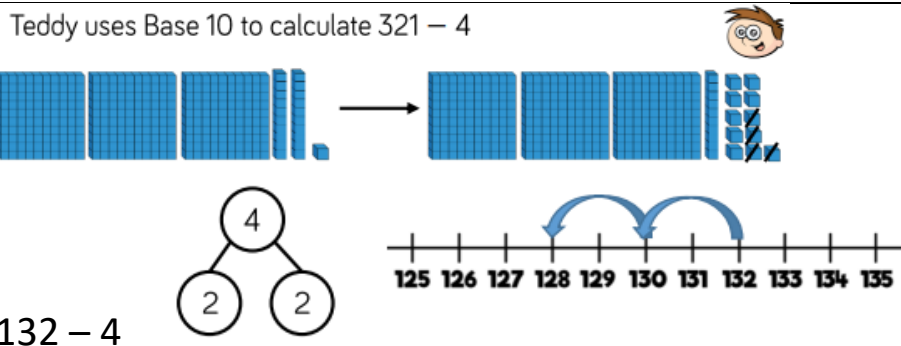
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| | <ul style="list-style-type: none">• Children will be encouraged to recognise the subtraction structure of difference by solving contextual problems involving finding a difference eg I have £19 and I want to buy a game which costs £25. How much more money do I need? ($£25 - £19 = £6$) |
|--|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

Year 3

Objective and Strategy	Models and Representations - CPA						
<p>Subtract Multiples of 100</p> <p>Children will apply their prior knowledge of subtracting ones and tens to subtracting multiples of 100. Using concrete manipulatives and pictorial representations throughout is important so the children can see the value of the digits.</p> <p>A range of familiar representations of a given calculation are used alongside the column-subtraction layout so that children see the relationship between the numbers.</p>	<div><div><div>375 - 300 = 75</div></div><div><div>375 - 300 = 75</div></div></div>						
<p>Subtract 3-digit and 1-digit numbers – not crossing 10</p> <p>During this small step, children subtract ones from a 3-digit number without an exchange.</p>	<table border="1"><thead><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td></td><td></td><td></td></tr></tbody></table> <div>214 - 3 = ____</div> <div><div>356 - 5 =</div><div>357 - 5 =</div><div>358 - 5 =</div><div>359 - 5 =</div></div>	Hundreds	Tens	Ones			
Hundreds	Tens	Ones					
							

Subtract 1-digit from 3-digits- crossing 10

Children subtract 1-digit from a 3-digit number using an exchange. Children need to be secure in the fact that 321 is 3 hundreds, 2 tens and 1 one but that it is also 3 hundreds, 1 ten and 11 ones.



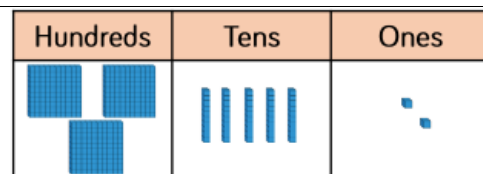
$$132 - 4$$

$$123 - 8 = ?$$

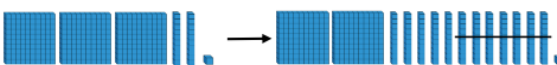
Subtract 2-digits from 3-digits

Children subtract multiples of 10 from a 3-digit number, first without and then with an exchange. The examples show different ways this concept could be taught using number lines and part-whole models.

The column method could be used, however it is not the most efficient method. Counting backwards in tens or using 100 to help will support mental strategies.

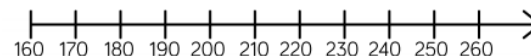


$$352 - 2 \text{ tens} =$$



$$321 - 70 = 251$$

Count back in tens to solve $240 - 70$



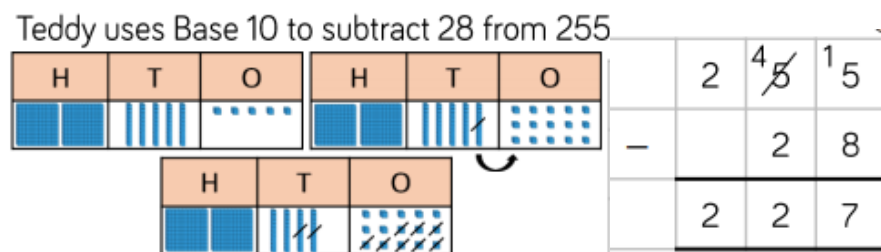
Amir calculates $425 - 90$ by subtracting 100 and then adding 10

$$425 - 100 = 325$$

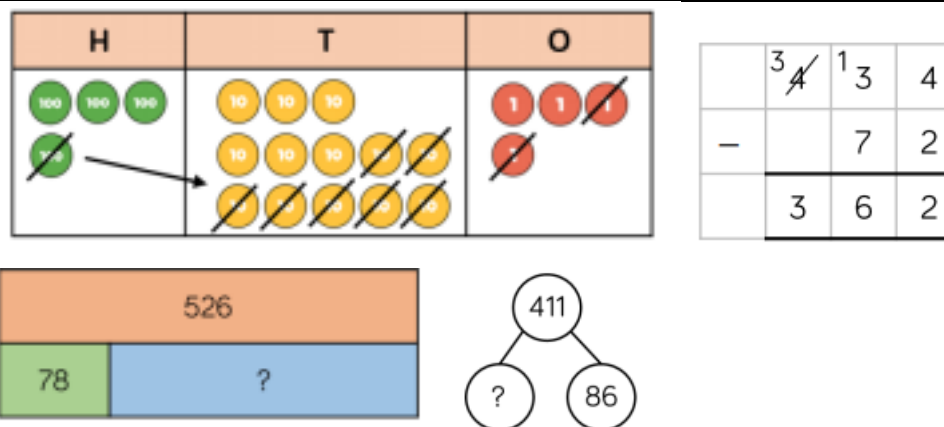
$$325 + 10 = 335$$

Subtract 2-digits from 3-digits (2)

Children focus on the position of numbers and place value to subtract 2-digits from 3-digits using the column method. Children start by exchanging one ten for ten ones. Next they exchange one hundred for ten tens before subtracting numbers where there are exchanges in both columns. Children are encouraged to use Base 10 and place value counters so they can physically exchange



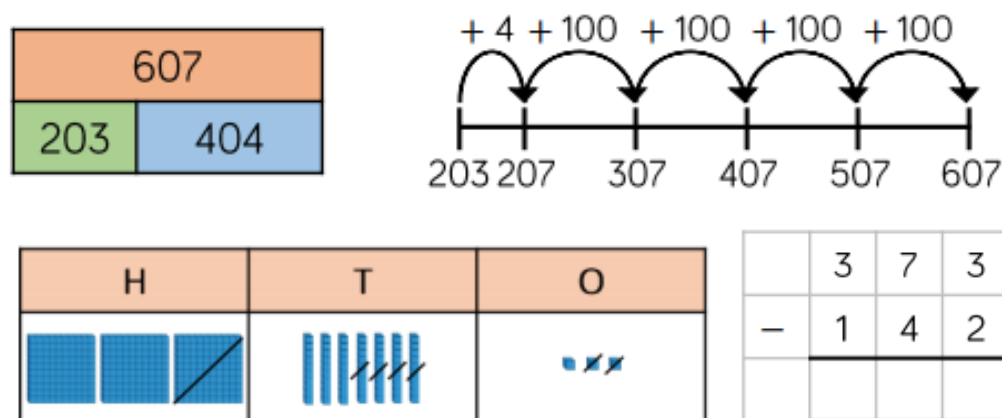
and see the link between the concrete and the written column method.



Subtract 3-digits from 3-digits (1)

It is important for the children to understand that there are different methods of subtraction. They need to explore efficient strategies for subtraction, such as counting on (number lines), near subtraction and number bonds.

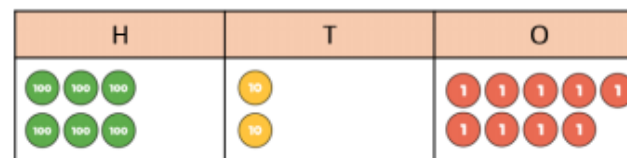
They then move on to setting out formal column subtraction supported by practical equipment.



Subtract 3-digits from 3-digits (2)

Children explore column subtraction using concrete manipulatives. It is important to show the column method alongside so that children make the connection to the abstract method and so understand what is happening. Children progress from an exchange in one column, to an exchange in two columns. The importance of recording any exchanges clearly in the written method is reinforced.

$$629 - 483$$



	H	T	O
	6	8	3
-	4	8	3

Further Notes

- Children should count regularly, on and back, including multiples of 4, 8, 50 and 100 and steps of 1/10.
- Children will regularly practise fluency in subtraction facts within and across 10 to support their understanding in column subtraction.
- Children should continue to partition in different ways to help to support subtraction.
- Children will be encouraged to choose the mental strategies which are the most efficient for the numbers involved.
- Children will continue to practise recall of appropriate doubles and halving facts to support calculations such as $18-9=9$.

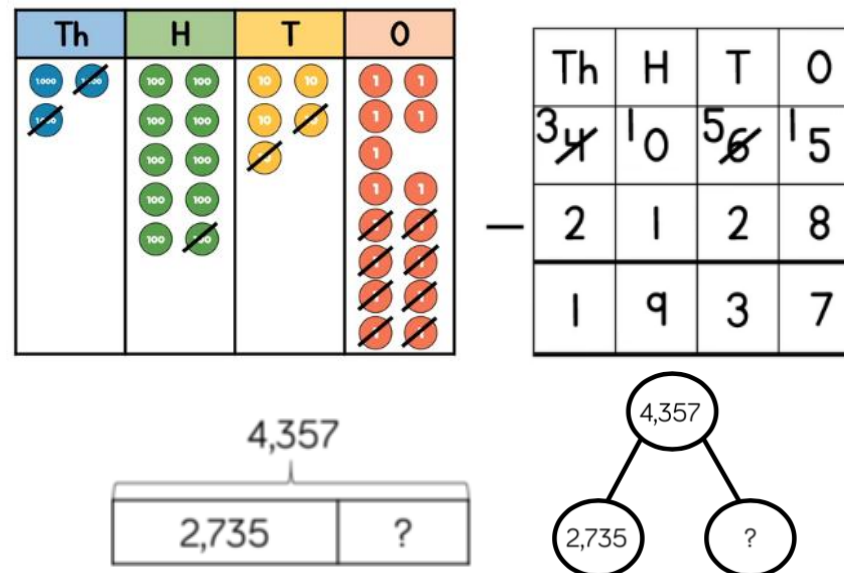
Year 4

Objective and Strategy	Models and Representations - CPA																				
Subtract two 4-digit numbers – no exchange (1) Building on their experiences in Year 3, children use their knowledge of subtracting using the formal column method to subtract two 4-digit numbers. Children will focus on calculations with no exchanges, focusing on the value of each digit.	<div><div><div><div>Th</div><div><div><div>1000</div><div>1000</div><div>1000</div></div></div></div><div>H</div><div><div><div>100</div><div>100</div><div>100</div></div><div><div><div>100</div><div>100</div></div></div></div><div>T</div><div><div><div>10</div><div>10</div><div>10</div></div><div><div><div>10</div><div>10</div></div></div></div><div>O</div><div><div><div>1</div><div>1</div><div>1</div><div>1</div></div><div><div><div>1</div><div>1</div><div>1</div><div>1</div></div></div></div></div></div> <div><table><tr><td></td><td>Th</td><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td>3</td><td>4</td><td>5</td><td>4</td></tr><tr><td>–</td><td>1</td><td>2</td><td>2</td><td>4</td></tr><tr><td></td><td>2</td><td>2</td><td>3</td><td>0</td></tr></table></div>		Th	H	T	O		3	4	5	4	–	1	2	2	4		2	2	3	0
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Subtract two 4-digit numbers – one exchange (2) Children continue to use their knowledge of subtracting using the formal column method to subtract two 4-digit numbers. Children explore subtractions where there is one exchange. They use place value counters to model the exchange and match this with the written column method.	<div><div><div><div>1,000s</div><div><div><div>1000</div><div>1000</div><div>1000</div><div>1000</div></div></div></div><div>100s</div><div><div><div>100</div><div>100</div><div>100</div><div>100</div></div><div><div><div>100</div><div>100</div></div></div></div><div>10s</div><div><div><div>10</div><div>10</div><div>10</div><div>10</div></div></div><div>1s</div><div><div><div>1</div><div>1</div><div>1</div></div><div><div><div>1</div><div>1</div><div>1</div></div></div></div></div></div> <div><div><div><div>1,000s</div><div><div><div>1000</div><div>1000</div><div>1000</div><div>1000</div></div></div></div><div>100s</div><div><div><div>100</div><div>100</div><div>100</div><div>100</div></div><div><div><div>100</div><div>100</div></div></div></div><div>10s</div><div><div><div>10</div><div>10</div><div>10</div><div>10</div></div><div><div><div>10</div><div>10</div></div></div></div><div>1s</div><div><div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div></div><div><div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div></div></div></div></div></div> <div><div><div><div>1,000s</div><div><div><div>1000</div><div>1000</div><div>1000</div><div>1000</div></div></div></div><div>100s</div><div><div><div>100</div><div>100</div><div>100</div><div>100</div></div><div><div><div>100</div><div>100</div></div></div></div><div>10s</div><div><div><div>10</div><div>10</div></div><div><div><div>10</div><div>10</div></div></div></div><div>1s</div><div><div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div></div><div><div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div></div></div></div></div></div> <div><table><tr><td></td><td>Th</td><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td>5</td><td>6</td><td>3</td><td>13</td></tr><tr><td>–</td><td>4</td><td>3</td><td>1</td><td>6</td></tr><tr><td></td><td>1</td><td>3</td><td>2</td><td>7</td></tr></table></div>		Th	H	T	O		5	6	3	13	–	4	3	1	6		1	3	2	7
	Th	H	T	O																	
	5	6	3	13																	
–	4	3	1	6																	
	1	3	2	7																	

Subtract two 4-digit numbers – more than one exchange (3)

Children explore what happens when a subtraction has more than one exchange. They can continue to use manipulatives to support their understanding. Some children may feel confident calculating with a written method.

Children will be encouraged to continue to explain their working to ensure they have a secure understanding of exchange within 4-digit numbers.

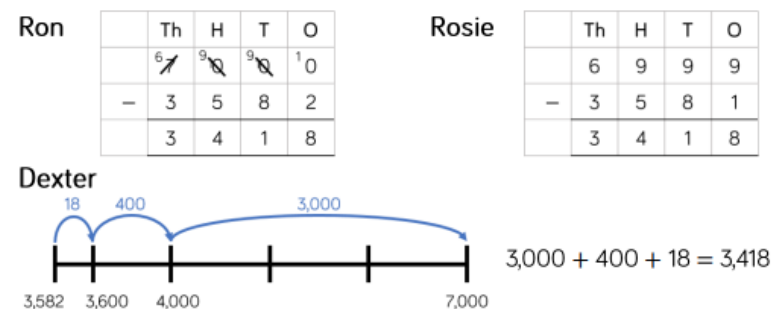


Efficient Subtraction

Children use their understanding of column subtraction and mental methods to find the most efficient methods of subtraction. They compare the different methods of subtraction and discuss whether they would partition, take away or find the difference.

Ron, Rosie and Dexter are calculating $7,000 - 3,582$

Here are their methods:



Whose method is most efficient?

Use the different methods to calculate $4,000 - 2,831$

Further Notes

- Children should continue to count regularly, on and back, now including multiples of 6, 7, 9, 25 and 1000 and steps of 1/100.
- Children should continue to partition numbers in different ways.
- They will be encouraged to choose from a range of strategies, exploring which is the most efficient method for a given subtraction such as counting forwards or backwards, partitioning, using column subtraction, using known facts such as 'near' doubles or place value.